

Original Article

Triplet Sensors in Towed Array Sonar Systems

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Abstract - Cardioid or triplet towed arrays are used in sonar applications to resolve left/right ambiguity by placing a null in the ambiguous direction. It leaves an uncalibrated residual signal in the opposite direction from which the desired signal arrives. In the sonar signal processing, the weighted delayed sum beam forming is used to discriminate between signal arrival from different bearings; however, in the towed linear array, there will be a symmetry in signal arrival delays produced from acoustic signal arriving from two distinct directions one being on the left side and other beings on right side of the array resulting in left /right ambiguity. Here Cardioid or triplet arrays consisting of a line of triplets instead of a line of single hydrophones are used. Each triplet consists of three closely-spaced omnidirectional hydrophones evenly mounted on a circle perpendicular to the array axis.

Keywords - Cardioid, Hydrophones, Omnidirectional, Sensor, Triplet array.

1. Introduction

The Towed array of sonars consists of a Wet end subsystem. Onboard electronics subsystems have sonar signal processing modules, post-signal processing modules, Sonar HMI modules and a launch and recovery system (Winch) for deploying/retrieving the towed subsystem. The advantages of Towed Array-based sonar over the Hull mounted array sonar are variable depth operation capability to mitigate layer problems and exploit SOFAR channels in the sea. Another advantage is the larger aperture for the sensor system allowing low-frequency operation and long-range capability.

The beam forming followed by energy detection is the signal processing technic is used to obtain the direction of arrival of the signal. Beamforming in the time domain is generally done by applying the weighted delayed sum of the array of hydrophone (sensors) outputs placed in the towed array sensor system. However, due to symmetry in the linear nature of Towed array toward signals arriving from the left side and right side, every angle on the left side will have a corresponding angle on the right side which has a similar set of delays at hydrophone points.

The Towed array systems should have the arrangement of sensor systems which allows us to form unidirectional beams, this formation of unidirectional beams will logically produce the effect of having two directional sensors, one looking towards the left side and the other looking towards the right side of the array.

2. Materials and Methods

2.1. Triplet Array

The Cardioid beam forming can be used to solve the inherent L/R ambiguity resolution problem in towed array sonar systems. The Cardioid beam forming uses the Triplet array sensor instead of one single-line array. The triplet array system consists of closely spaced hydrophone elements spaced 120° apart. The signal processing technique can be employed to convert the triplet array into logically two directional hydrophone systems, one looking towards the left and the other towards the right is understanding the Design, Manufacturing and Use of the products and build robustness into the product so that the product continues to function satisfactorily under the encountered stresses. Each triplet element consists of closely spaced omnidirectional hydrophone sensors placed in a single housing, evenly mounted on a circle perpendicular to the array axis. Referenced on the right-handed Cartesian system (X, Y, Z), Y is the array axis pointing at the towing direction; the X axis points at the starboard broadside and the Z axis points at the sea surface, as shown in Fig. 1. Let K be the number of triplets in the array and let $k = 1, 2, \dots, K$ be the triplet index.

Similarly, let $j = 1, 2, 3$ be the index of the hydrophones within each triplet. The angular separation between the equally-spaced triplet sensors is denoted as γ , where $\gamma = 2/3\pi$ (120°). Due to forces applied to the array during the tow, the array is often twisted concerning its original deployment position. The twist angle of the k-th triplet is denoted as β_k and is defined clockwise concerning the Z axis. Then the angles of each sensor concerning Z can be defined as follows:

$$\begin{aligned}\phi_{1k} &= \beta_k \\ \phi_{2k} &= \beta_k + \gamma \\ \phi_{3k} &= \beta_k - \gamma\end{aligned}\quad (1)$$



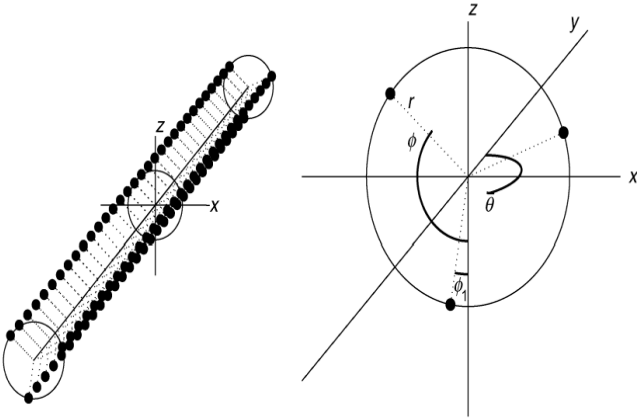


Fig. 1 Geometry of hydrophone triplet

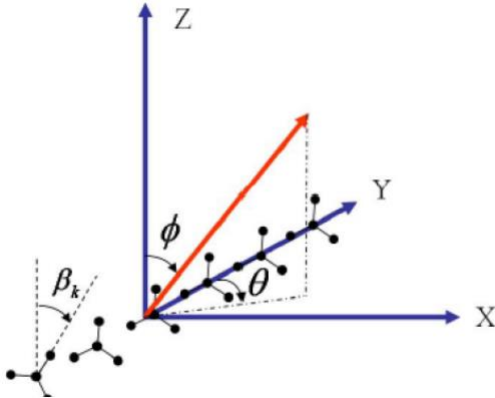


Fig. 2 Triplet Array in Cartesian Co-ordinates

As per this notation, the vector v_{jk} is defined to locate the j th hydrophone in the k th triplet element.

$$v_{jk} = \begin{bmatrix} r \sin \phi_{jk} \\ y_k \\ r \cos \phi_{jk} \end{bmatrix} \quad (2)$$

Here r is the circle's radius in the triplet housing system in which three hydrophones are mounted at 120° apart, and y_k is the Y coordinate of the k th triplet element. Rolling sensors are used across the towed array to measure the twist in the array, and necessary shape correction can be employed for the triplet array before signal processing.

2.2. Cardioid Beamforming

Cardioid beam forming resolves the port/ starboard ambiguity problem in towed arrays. The Cardioid beam pattern is obtained from the normal single line array beam pattern by weighing the beam pattern of the line array with

the help of the cardioid-shaped function, which places the null at the ambiguous side. The time domain method of cardioid beam forming is explained below. Let us consider (θ, ϕ) is steering direction, where θ is the azimuth angle (clockwise) on the X - Y plane, and ϕ is the elevation angle (from vertical) in the X - Z plane. The unit vector $u(\theta, \phi)$ is defined below.

$$u(\theta, \phi) = \begin{bmatrix} \sin \phi \sin \theta \\ \sin \phi \cos \theta \\ \cos \phi \end{bmatrix} \quad (3)$$

The signal received on the triplet hydrophone element is related in the following way.

$$s_{jk} = s_k(t - d_{jk}) \quad (4)$$

Where,

$$d_{jk} = \frac{\{u(\theta, \phi) \cdot v_{jk}\}}{c} \quad (5)$$

The time delay between the triplet phones is defined by the ratio of the projection of v_{jk} on $u(\theta, \phi)$ to the sound speed where the scalar operator is, i.e. the inner product of the two vectors given by the following equation.

$$\{u(\theta, \phi) \cdot v_{jk}\} = r(\sin \phi_{jk} \sin \phi \sin \theta + y_k \sin \phi \cos \theta + \cos \phi_{jk} \cos \phi) \quad (6)$$

By considering the triplet element at the origin, it becomes that $y_k = 0$, so the inner product gets simplified to

$$\{u(\theta, \phi) \cdot v_{jk}\} = r(\sin \phi_{jk} \sin \phi \sin \theta + \cos \phi_{jk} \cos \phi) \quad (7)$$

The main idea behind the cardioid beam forming is to suppress the signal from an ambiguous direction. The former beam output in cardioid beam forming is given by

$$b_{jk}(\theta, \phi) = \sum_{j=1}^3 s_{jk}(t - d_{jk}) \{u(\theta, \phi) \cdot v_{j,k}\} \quad (8)$$

Using S_{jk} given by (4), output due to the signal coming from the desired direction becomes,

$$b_{jk}(\theta, \phi) = \sum_{j=1}^3 s_{jk}(t - 2d_{jk}) \{u(\theta, \phi) \cdot v_{j,k}\} \quad (9)$$

The signal arriving from an ambiguous direction will have the following relation,

$$s_{jk} = s_k(t + d_{jk}) \quad (10)$$

Using S_{jk} given by (10), output due to the signal coming from an ambiguous direction becomes

$$b_k(\theta, \phi) = \sum_{j=1}^3 s_{jk}(t) \{u(\theta, \phi) \cdot v_{j,k}\} \quad (11)$$

Or equivalently

$$b_k(\theta, \phi) = s_{jk}(t) \sum_{j=1}^3 \{u(\theta, \phi) \cdot v_{j,k}\} = 0 \quad (12)$$

3. Results and Discussion

3.1. Array Element Simulation

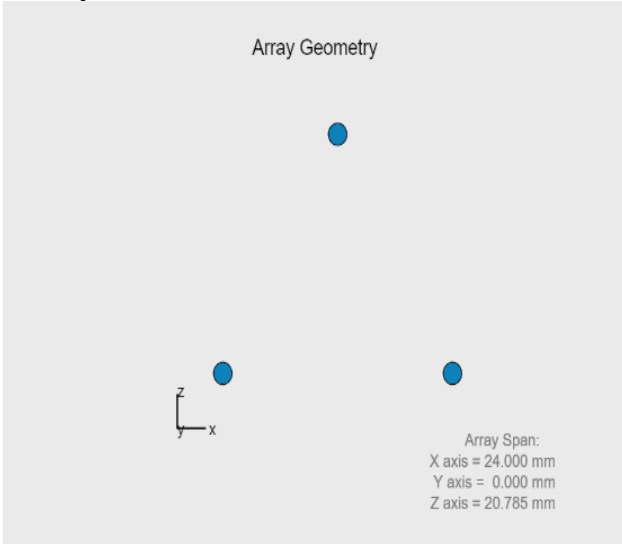


Fig. 3 Array element geometry in Phased Array MATLAB Tool Box

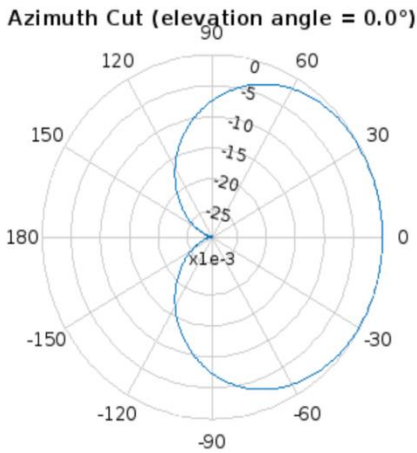


Fig. 4 Cardioid Beam former output from single Triplet element at the broad side

3.2. Single Line Array Simulation

Initially, a study case of 32 hydrophone elements single line array is simulated using an omnidirectional sensor system.

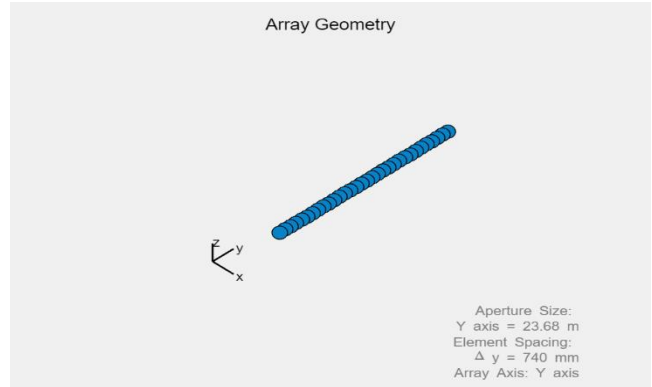
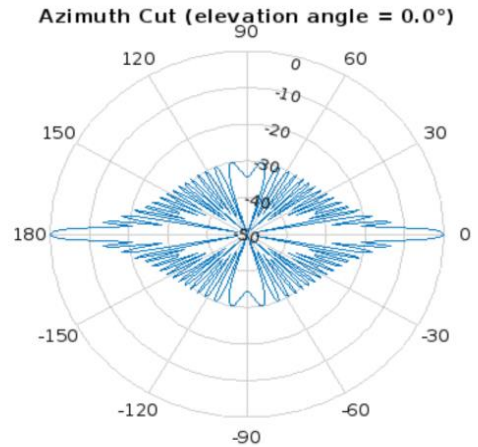


Fig. 5 Single Line Array in Phased Array Matlab Tool Box



= Normalized Power (dB), Broadside at 0.00 °

Fig. 6 Beam former output for broadside, having left/Right ambiguity

3.3. Triplet Array

The array of triplet elements is constructed in Matlab phased array toolbox. Cardioid beam forming is carried out to obtain the directional response with a better 3dB response. The cardioid beam forming is carried out at each triplet element level to convert each element into a single directional hydrophone. Then, delayed sum beamforming is applied over the array of these logically directional hydrophones to obtain the steered response with better 3dB performance.

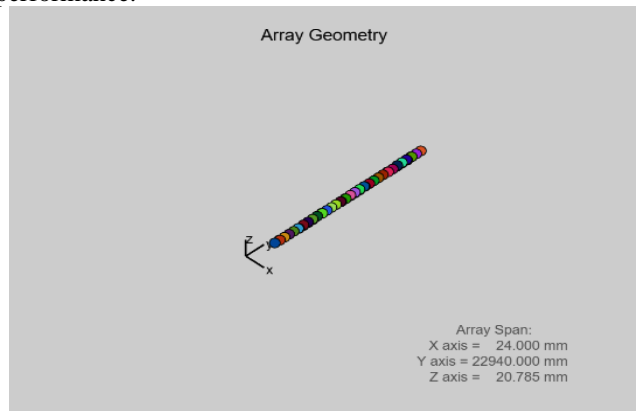


Fig. 7 Array of Triplet Elements in Phased Array Tool Box

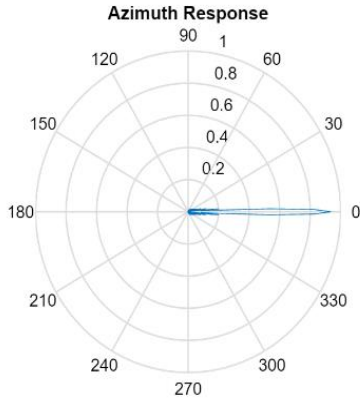


Fig. 8 Cardioid Beam former output from Array Triplet elements

The array of triplet elements is constructed in Matlab phased array toolbox, and Cardioid beam forming is carried out to obtain the directional response with a better 3dB response. Here, the cardioid beam forming is carried out at each triplet element level to convert each element into a single directional hydrophone. Then, delayed sum beamforming is applied over an array of these logically directional hydrophones to obtain the steered response with better 3dB performance.

The output from the cardioid beamformer that is displayed on the display cabinet of the towed array sonar is shown. It can be observed that the port/starboard ambiguity, which downgrades active sonar performance, is rectified. The Port Starboard discrimination is very good.

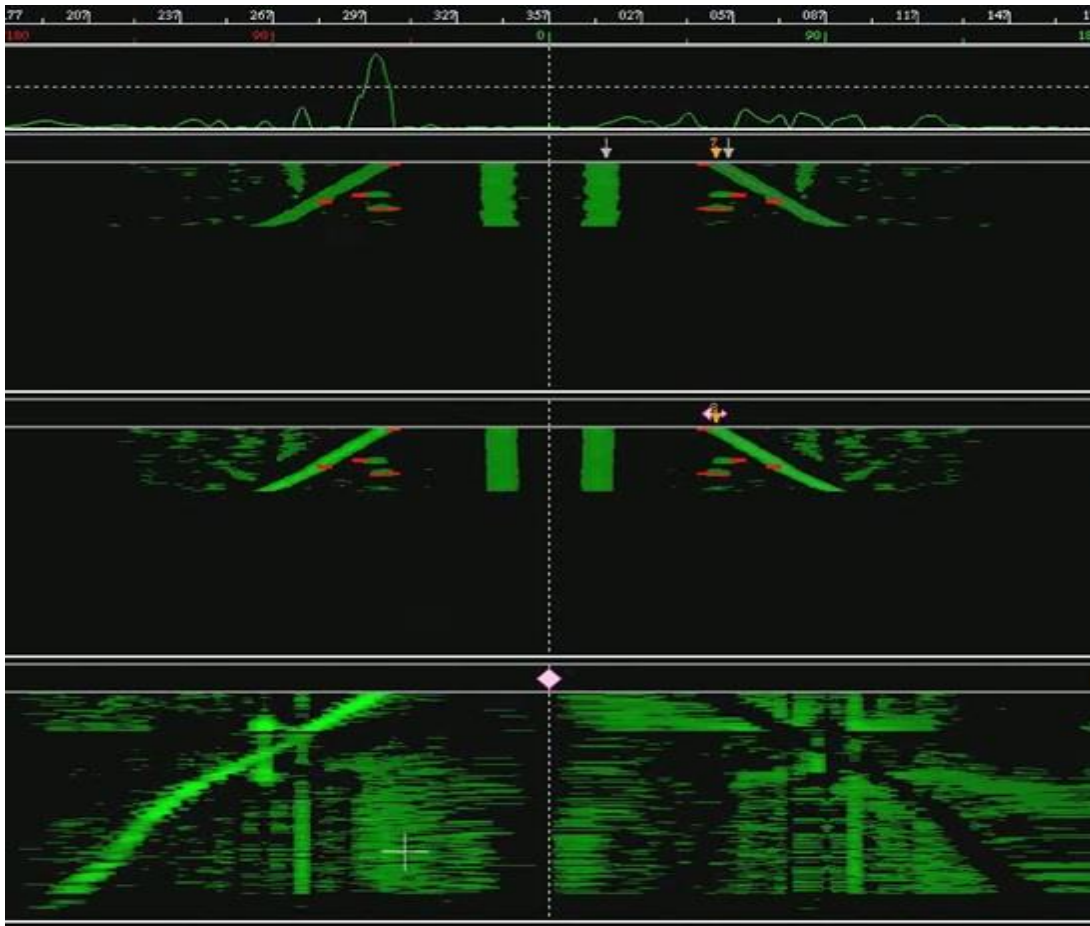


Fig. 9 Cardioid beamformer output on the display cabinet of the towed array sonar

4. Conclusion

Single Line arrays have inherent Left / Right Ambiguity in Towed Array Sonar systems. Triplet Array in Towed Sonar systems can effectively solve the Left / Right Ambiguity problem in single-line Towed Array sonars. The output from the cardioid beamformer that is displayed on the

display cabinet of the towed array sonar is shown above. It can be observed that the port/starboard ambiguity, which downgrades active sonar performance, is rectified. The Port Starboard discrimination is very good. In future, the effective use of Cardioid beam forming along with a Quad array can be exploited to obtain Left /Right ambiguity resolution with high bearing accuracy and better 3dB performance

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